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| <b>Course Title:</b> Real and Functional Analysis   | <b>Number of Units:</b> 1 |
| <b>SSD :</b> MAT/05   | <b>CFU:</b> 9             |
| <b>Course aims:</b> The course aims to provide basic knowledge of Functional Analysis required to formulate mathematical models of engineering and scientific problems.   |                           |
| <b>Course Description:</b> Topological spaces. Metric spaces. Completeness. Compactness. Complete metric spaces: Banach spaces, Hilbert spaces. Orthonormal basis and Fourier series in Hilbert spaces. Linear and continuous operators between normed spaces. Compact operators. Adjoint operators. Spectral decomposition of self-adjoint operators. Spectrum of Laplace operator. Weak topologies. Reflexive spaces. Separable spaces. $L^p$ spaces. Sobolev spaces and variational formulation of boundary value problems for partial differential equations. Introduction to Galerkin methods and finite elements methods in a model case. |                           |
| <b>Assumed Background:</b> Mathematical Analysis at undergraduate level   |                           |
| <b>Assessment methods:</b> Oral examination   |                           |